

Lecture 11

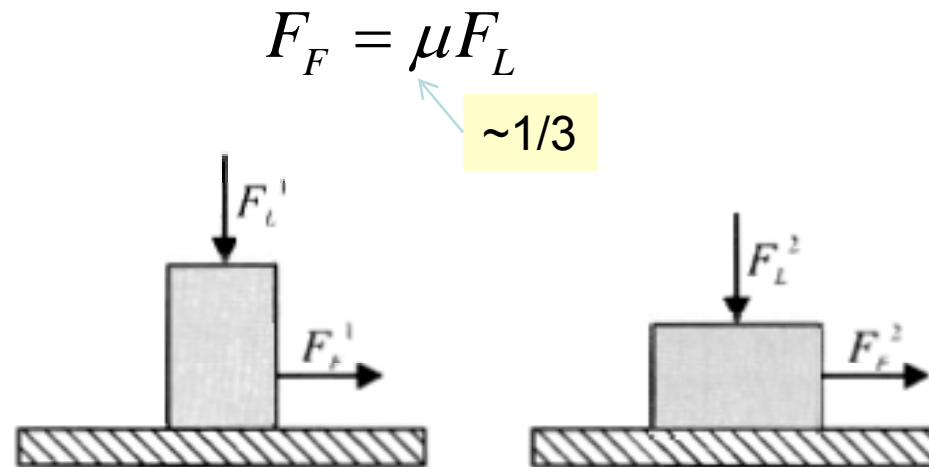
Friction, Lubrication and Wear

Definitions

- **Friction** – force between the interacting surfaces that resists or hinders their relative movement
 - Static friction – force to overcome to start movement
 - Dynamic friction – mechanical force between sliding or rolling surfaces
- **Wear** – progressive loss of materials caused by contact and relative movement
- **Lubrication** – aimed on reducing friction and minimizing wear
- **Tribology** – research field dealing with friction, lubrication and wear.

Amontons Law

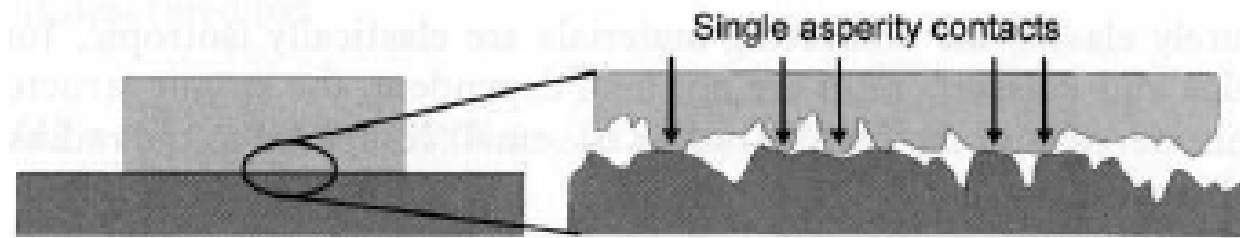
- in 1699 Guillaume Amontons found that the friction force is proportional to the load and doesn't depend on the contact area



- Amontons law is an empirical law, result of several physical phenomena acting at the same time

Amontons Law

- The real contact area is always smaller than the apparent one due to roughness



$$F_F = \tau_c \cdot A_{real}$$

yield stress during shear

- The real contact area can be measured e.g. using the electrical resistance of the interface or measure hotspots on a transparent solid with IR microscope

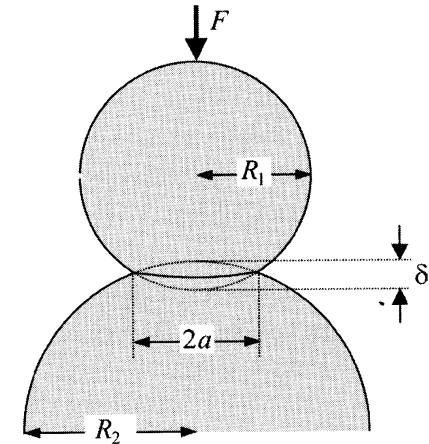
Possible origins for Amontons Law

- **Elastic deformation**

- Hertz law:

$$A_{real} \sim F_L^{2/3}$$

$$a^3 = \frac{3R^*}{4E^*} \cdot F_L$$



- Assuming Gaussian distribution of sphere sizes one can obtain a linear dependence between the load and the friction

- **Plastic deformation:**

- As load is applied the plastic deformation will start. It will continue till the pressure reaches some threshold

$$A_{real} \cdot P_m = F_L$$

- This gives again a linear dependence

Coulomb's law of friction

- Coulomb's law of friction:

The frictional force between the moving surfaces is independent on the relative speed

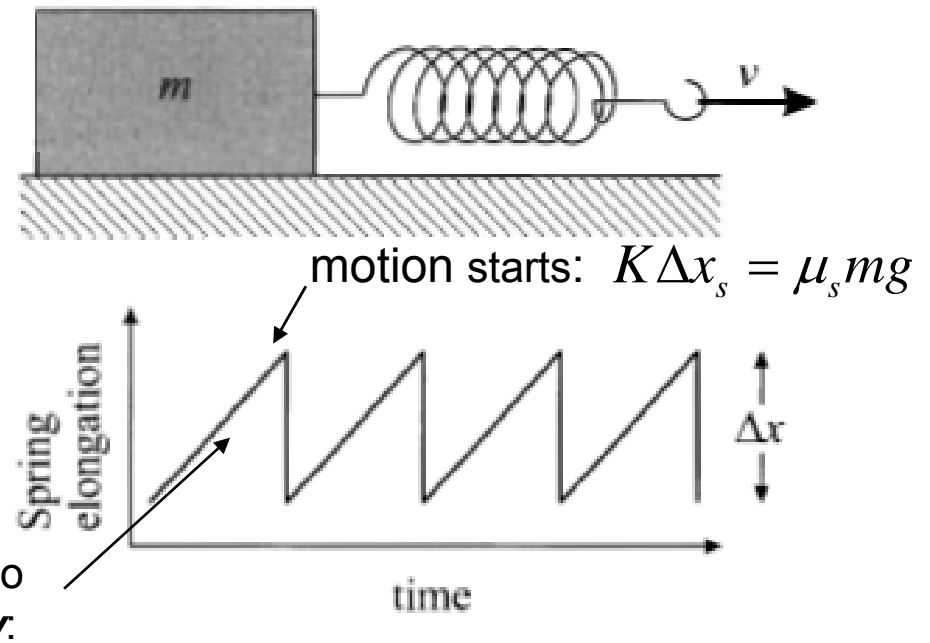
- Coulomb's law of friction is also counterintuitive as the friction is usually dependent on the speed, e.g. Stokes law

Static, kinetic and stick-slip friction

- Static friction:
 - friction force required to start motion,
 - higher than the dynamic friction
- Dynamic (kinetic) friction
 - force needed to sustain sliding
- Stick/slip motion
 - arises when the dragging force is coupled elastically to the sliding body e.g. excitation of a violin string by the bow, squeaking of doors and earthquakes
 - more pronounced at small velocities
 - increases with increasing difference between μ_s and μ_k .
 - more significant with soft springs
- For a block moving at constant velocity we expect:

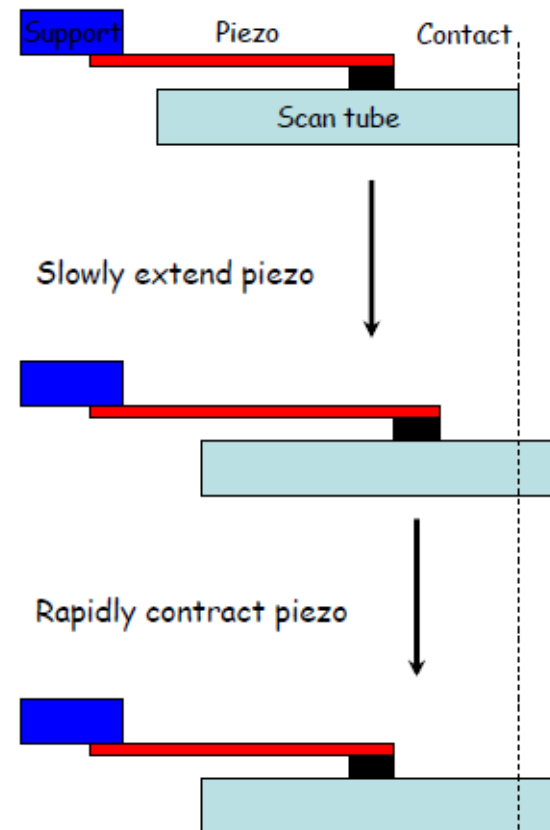
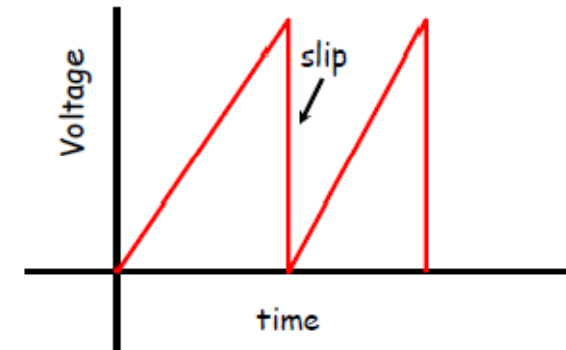
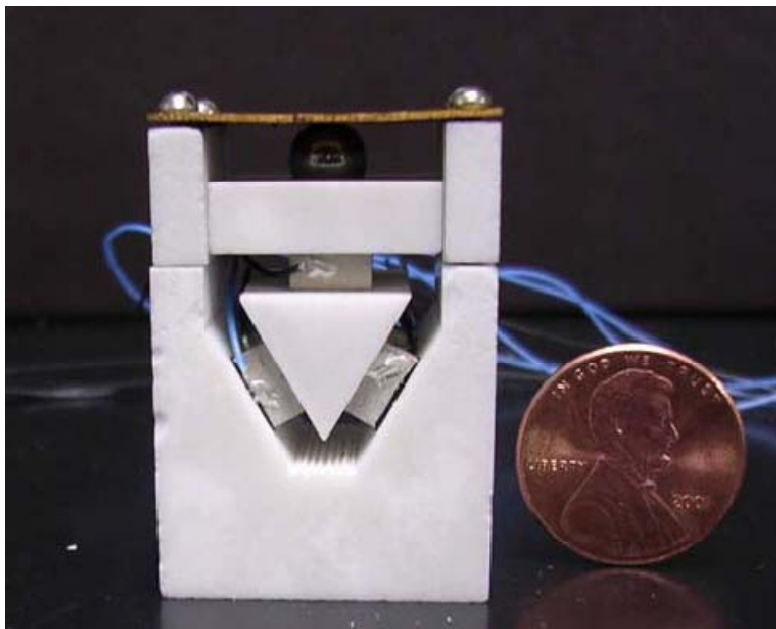
$$K \Delta x = \mu_k mg$$

- however at the start stick/slip motion can arise due to hysteresis in friction



Stick-slip motion in AFM/STM approach

- Applying a saw-tooth (or parabolic) waveform to a piezo a stick/slip motion can be achieved with fine ($<50\text{nm}$) reproducible steps up or down

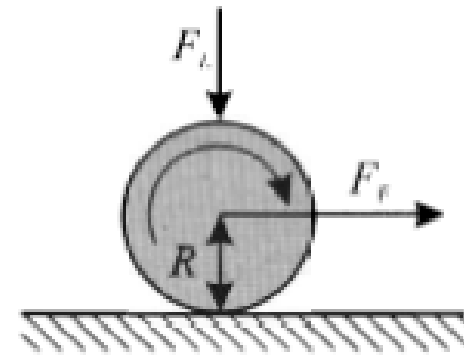


Rolling friction

- Force required to roll an object is usually much less than the one required to slide

$$M = F_F \cdot R = \mu_r F_L$$

torque of the rolling object



Rolling friction

- Rolling of infinitely hard sphere or cylinder should produce no friction.
- In real life there are several **sources of dissipation**:
 - Relative sliding (microslip) due to different elastic moduli of the bodies (seems to be relatively small as dependence on lubrication is usually weak)
 - Adhesion: continuous generation and breaking the contact, e.g. rolling on a sticky tape
 - Plastic deformation: if normal or tangential stress is too high plastic deformation can occur
 - Viscoelastic hysteresis: relaxation processes within the materials
- Rolling friction vs. speed:
 - soft sphere on a hard substrate: linear dependence
 - hard cylinder on viscous surface: initially increases to reach a maximum value and then decreases due to stiffening of material at high speeds

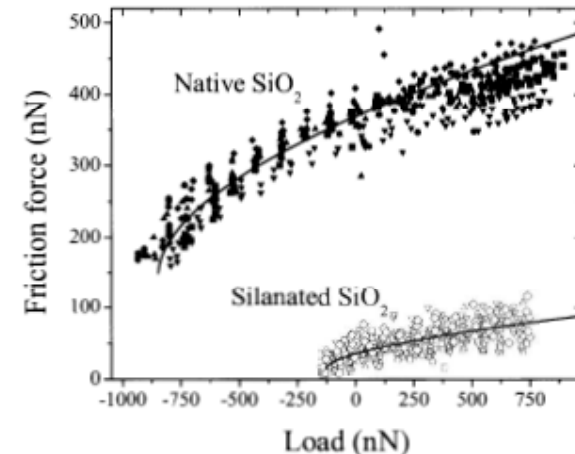
Friction and Adhesion

- Friction will become stronger if an adhesion, e.g. due to van de Waals forces is present

$$F_F = \mu (F_L + F_{adh})$$

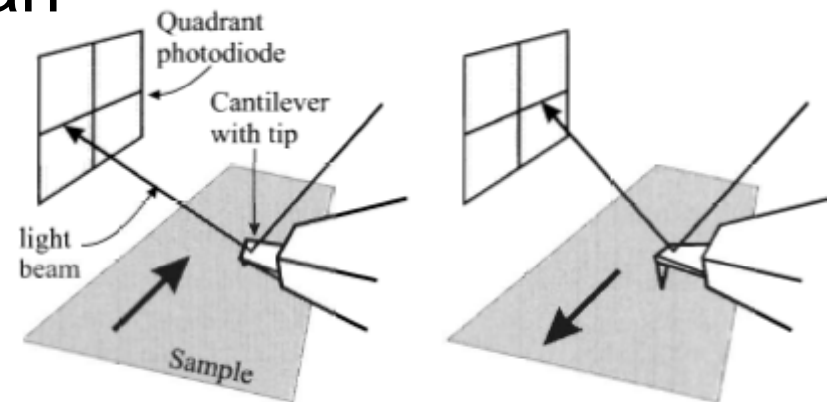
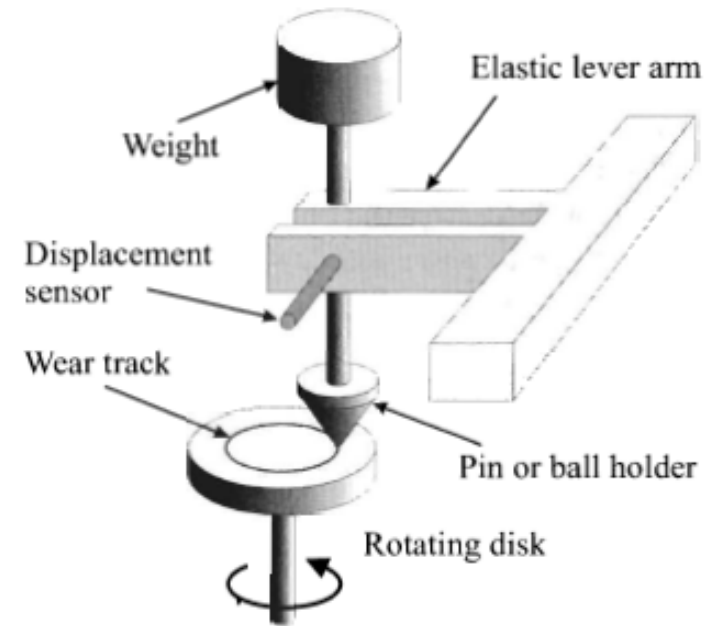
- As weight decreases as r^3 , for small objects this contribution is important.
e.g. for a $5\text{ }\mu\text{m}$ silica sphere gravity force 1.9pN and the adhesion force is measured about of 850 nN

Amontons law is not valid for small contact areas



Measuring friction

- Classical devices to measure friction force called **tribometers**. Easiest approach to measure drag force with known load force
- Static force is measured with inclined plane tribometers
- Dynamic friction is measured with pin-on-disk tribometers
- Friction on nanometer scale can be measured with later force (friction) microscopy, LFM
- Damping in QCM is related to slip time of weakly adsorbed layers



Macroscopic friction

- macroscopic friction depends on the nature of the surface:
 - clean metals: $\mu=3-7$
 - oxides: $\mu=0.6-1$
- friction coefficient depends on load, e.g. due to penetration through the surface oxide
- friction coefficient might depend on time in case of plastic deformation:

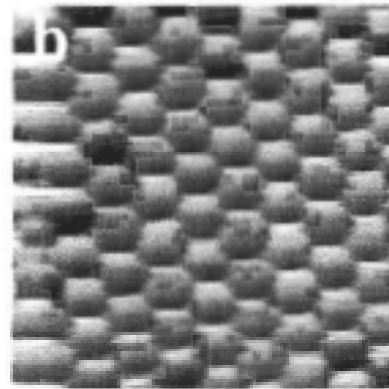
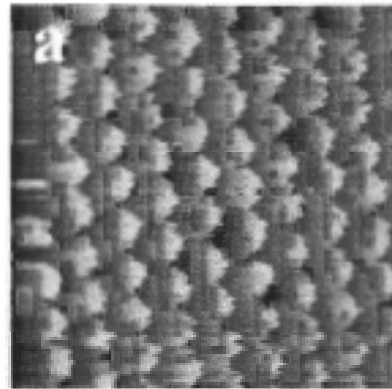
creeping increase in contact area: $\Delta A_{real} \propto \ln(1 + t / \tau)$

- friction coefficient might depend on local (surface) melting as well as surface phenomena e.g. friction on ice $\mu=0.03$

Microscopic friction

- Atomic stick/slip motion observed on a number of atomically flat materials: graphite, NaF, NaCl, AgBr, MoS₂ etc.
- LFM imaging on a graphite

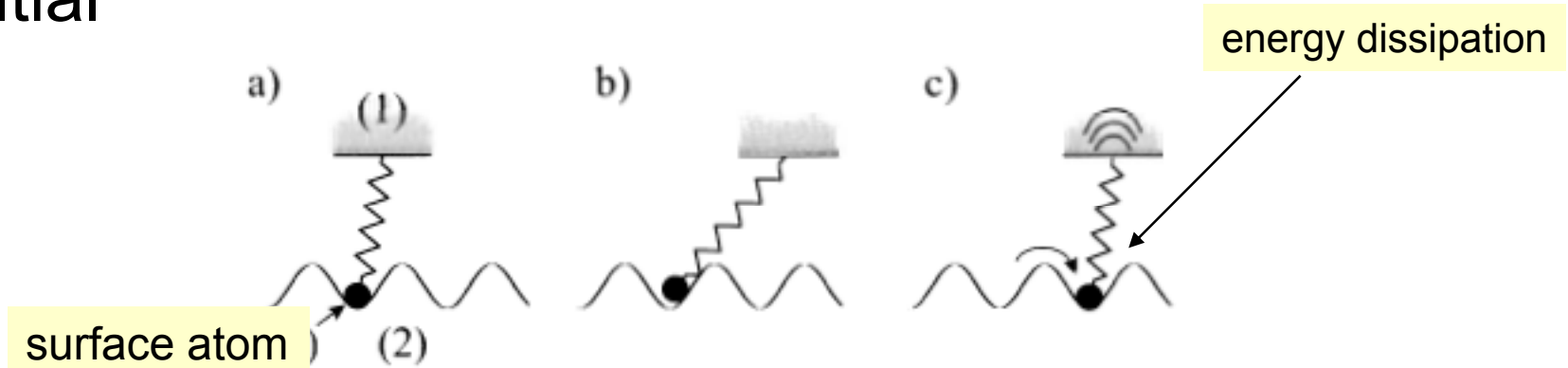
parallel to scan
direction



perpendicular to
scan direction

Microscopic friction

- **Tomlinson model:** wearless friction due to periodic potential



- explains the Coulomb friction law (independence on the velocity)

$$m_x \ddot{x} = K(x_0 - x) - \frac{\partial V(x, y)}{\partial x} - \gamma_x \dot{x}$$

$$m_y \ddot{y} = K(y_0 - y) - \frac{\partial V(x, y)}{\partial y} - \gamma_y \dot{y}$$

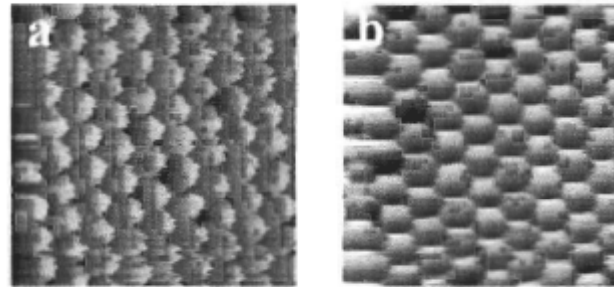
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Microscopic friction

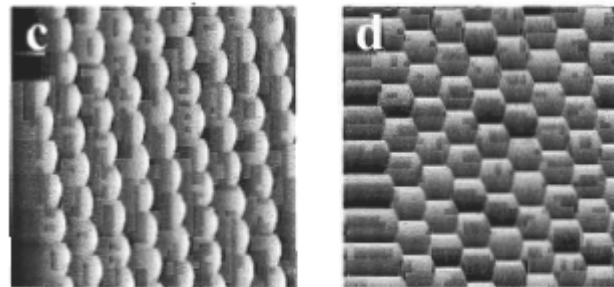
- Modeling the atomic stick-slip motion:

$$V(x, y) = -V_0 \left[2 \cdot \cos\left(\frac{2\pi}{a} x\right) \cos\left(\frac{2\pi}{a\sqrt{3}} y\right) + \cos\left(\frac{2\pi}{a\sqrt{3}} y\right) \right]$$

experiment



model



Microscopic friction

- The loss mechanism can be related to electronic and phononic contribution depending on the material, temperature etc.
- at the nanoscale, the real and apparent area are the same, continuum theories like JKR can be applied to determine the actual contact area
- due to small curvature, AFM tips can penetrate through the lubrication layer

Lubrication

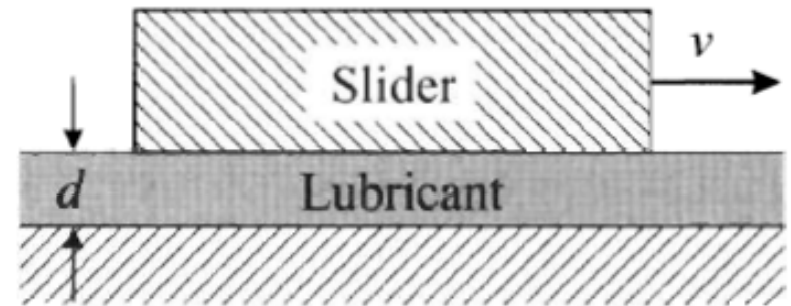
- Lubrication reduces friction and, correspondingly, wear.
- Lubrication regimes (depending on thickness):
 - **hydrodynamic lubrication:**
lubrication layer is higher than the height of surface asperities
 - **boundary lubrication:**
lubrication layer is just few molecular layers thick, thinner than roughness
 - **mixed lubrication**

Hydrodynamic lubrication

- In the case of hydrodynamic lubrication, the friction is determined by fluid dynamics

$$F_F = A \cdot \tau_0 = A \cdot \eta \cdot \frac{v}{d}$$

- the assumptions:
 - laminar flow (typically the case, as d is about of $1\mu\text{m}$)
 - lubricant is a Newtonian liquid



Hydrodynamic lubrication: comments

- Practically, the increase of viscous friction with velocity is slower than predicted by NS, presumably due to local temperature increase

$$\eta = \eta_0 \cdot \exp(E/kT)$$

also, friction is reduced at higher temperatures

- when pressure on the lubricant layer increases suddenly (like in chain-wheel gears) the lubricant is not expelled from the contact point: elasto-hydrodynamic lubrication
 - viscosity of most lubricants increases with pressure

$$\eta = \eta_0 \cdot \exp(\alpha P)$$

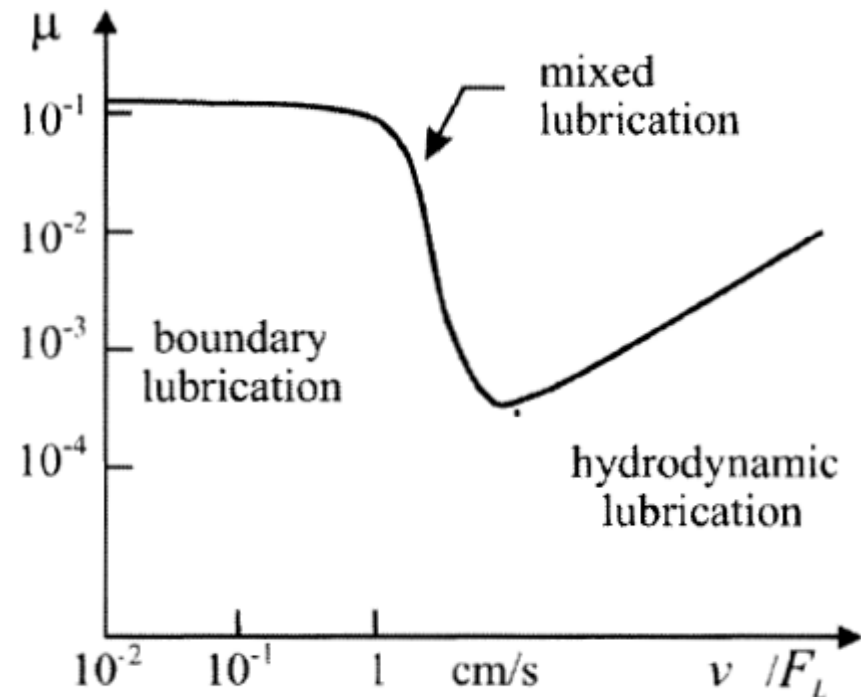
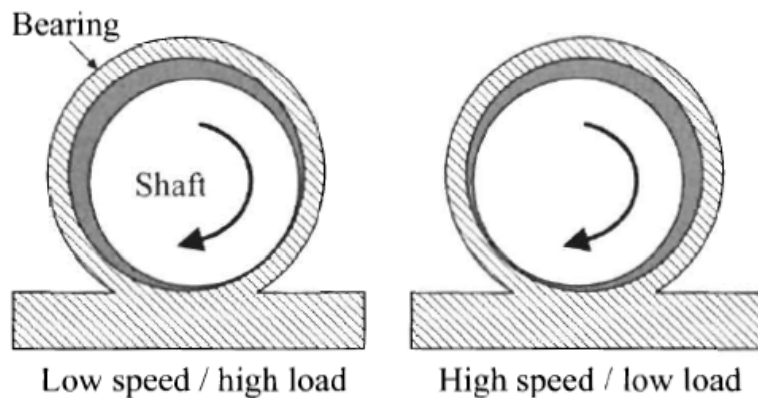
- solids deform elastically at high pressure, thin oil layer are getting stiff
- as a result, wear is reduced (except at start/stop) but repeated deformation of solids should be taken into account and could lead to failures

Boundary lubrication

- occurs at low sliding velocities and high loads when the lubricant is squeezed from the gap
- leads to higher friction (x100) than in the hydrodynamic regime
- the friction mainly depends on the nature of lubricant than on its viscosity
- important effect is reduction of adhesion, small Hamaker constant helps to reduce vdWaals forces between the surfaces.

Mixed lubrication

- Depending on the speed and load the same mechanism might be in the boundary, hydrodynamic or mixed regime:



Stribeck diagram

Thin film lubrication

- thin film lubrication – lubrication with films of molecular thickness.
- Non-DLVO effects related to (re-)ordering of molecular layers are important
- no-slip condition might be violated

Lubricants

- Major types of lubricants:
 - oil (petroleum or synthesis)
 - grease (oil + dispersion of a thickening agent)
 - solid lubricant (graphite, MoS_2)
- Characterized by
 - viscosity (viscosity index: kinematic viscosities at 40°C and 100°C compared to standard paraffin oil with weak T-dependence (100) and naphthenic oil with strong T-dependence (0))
 - volatility
 - ageing behavior (contamination, oxidation, thermal decomposition)

Wear

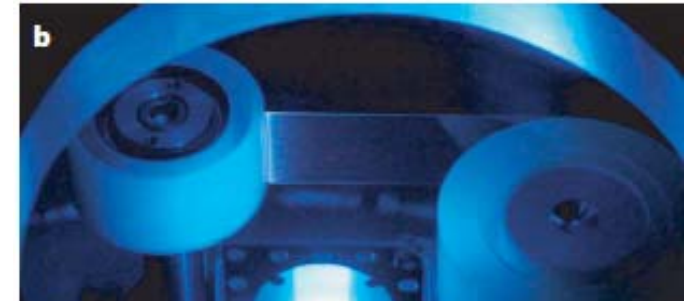
- Progressive loss of material from a body caused by contact and relative movement of a containing solid or liquid or gas

- Archard's law of adhesive wear $\Psi = k_w \cdot \frac{F_L v}{H}$
material loss hardness

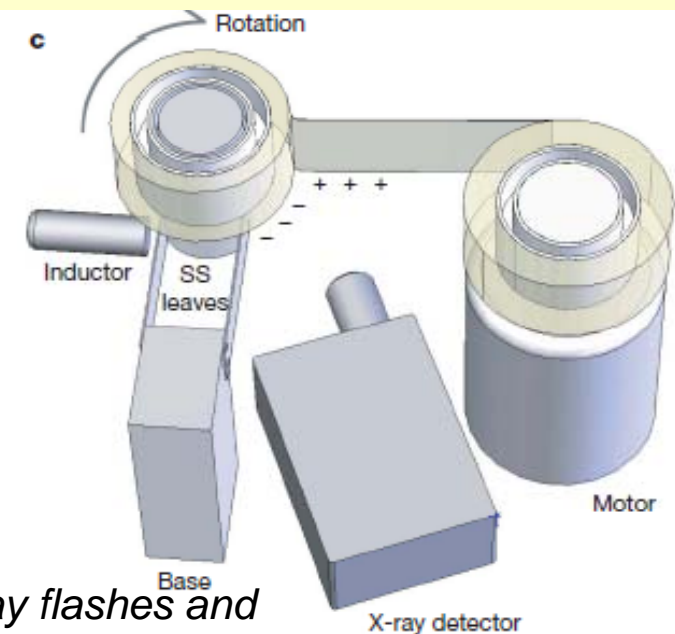
- Types of wear:
 - **abrasion**: wear in contact with harder material or hard particles
 - **erosion**: wear due to impingement by a stream containing solid particles (e.g. sand blasting)
 - **cold welding** effect due to adhesive contact
 - **surface fatigue** due to periodic load in the contact zone
 - **fretting wear**: in case of small oscillatory movement of the surfaces, the wear particles stay in the the contact area
 - cavitation caused wear, due to bubble formation
 - wear due to **tribochemical reactions** (caused by elevated temperatures, low energy electrons emission, removal of protective oxide layer, increase reactivity due to roughening, dangling bond, caused by plastic deformation).

Triboluminescence of a Scotch tape

- Breaking adhesion between two surfaces can produce significant energy in form of UV-VIS radiation and even X-rays (first discovered in 1939 and 1953, elaborated experiment in 2008)
- Suggested mechanism:
 - charge separation during peel-off the tape when positive charges left on acrylic adhesive and negative on the polyethylene roll
 - this eventually leads to a discharge
 - and Bremsstrahlung X-ray radiation



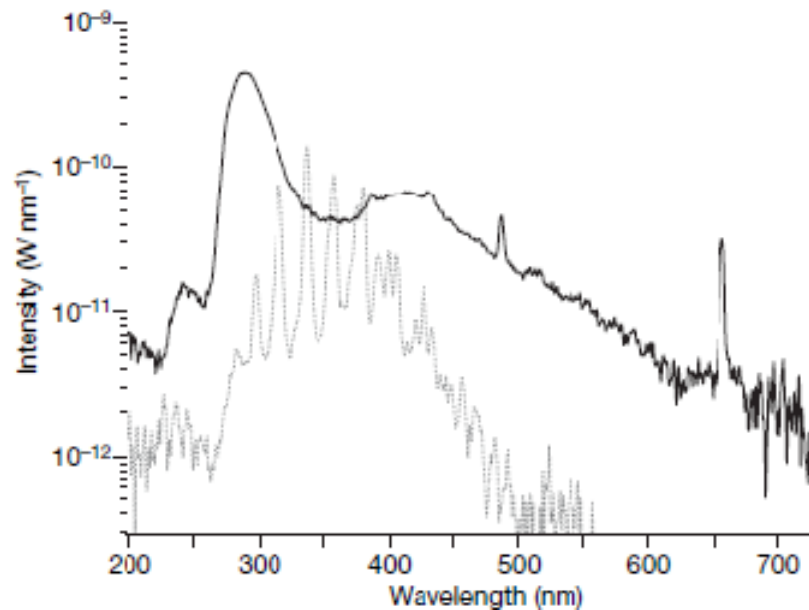
apparatus illuminated by scintillations



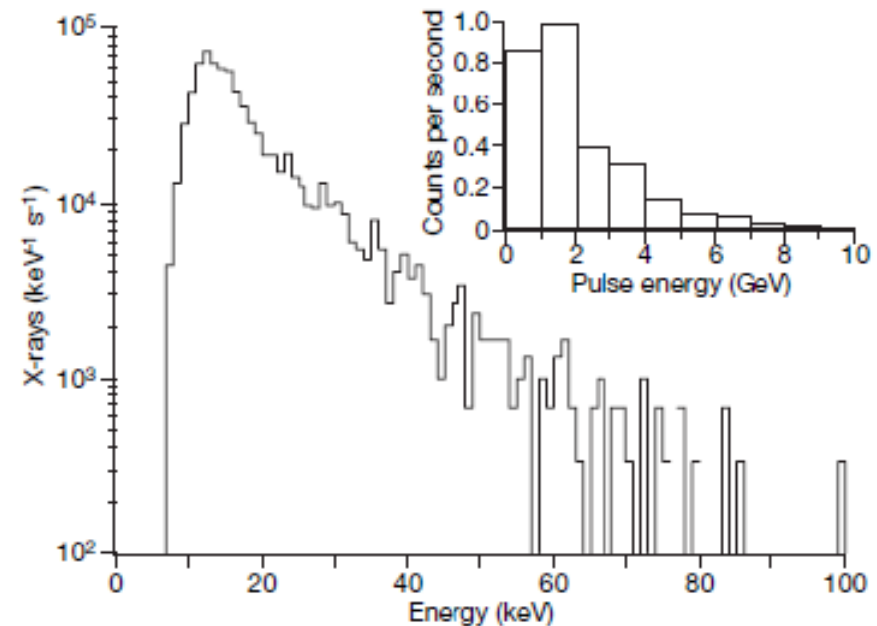
Carlos G. Camara et al, "Correlation between nanosecond X-ray flashes and stick-slip friction in peeling tape", *Nature* 455, 1089 (2008)

Triboluminescence of a Scotch tape

- Sufficient discharge currents power (0.2mW, estimated field $10^6 - 10^7$ V/cm, density 10^{11} - 7×10^{12} electron/cm², depending on the model)
- Can act as a simple source of X-rays sufficient for imaging applications



light spectra, in vacuum and in air, 1atm (gray)



X-ray spectra in vacuum

Carlos G. Camara et al, "Correlation between nanosecond X-ray flashes and stick-slip friction in peeling tape", *Nature* 455, 1089 (2008)

Problems

- End of chapter: 11.2, 11.3